Calibration of Satellite Measurements of River Discharge Using a Global Hydrology Model

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Abstract

Measurements of river discharge and watershed runoff are essential to water resources management, efficient hydropower generation, accurate flood prediction, and improved quantitative understanding of the global water cycle. Previous work demonstrates that orbital remote sensing can measure daily river discharge variation in a manner closely analogous to its measurement at ground stations, using reach flow surface area, instead of stage, as the discharge estimator. For international measurements, global hydrological modeling can be used to provide the needed calibration of incoming sensor data to discharge: our study tests this approach and investigates the accuracy of the results. We analyze 6 sites within the U.S. where co-located gauging station, satellite measurements, and model results are all available. Knowledge is thereby gained concerning how accurately satellite sensors can measure discharge, if the signal is calibrated only from global modeling results without any ground-based information.

Calibration (rating) equations for the remote sensing signal are closely similar whether based on gauging station or model information; $r^2$ correlation coefficients for least squares fits at one example site (#524; White River, Indiana) are both .66 ($n = 144$, monthly daily maxima, minima, and mean, 2003-2006). Space-based measurement of 4-day mean discharge at this site when using the model calibration is accurate to within +/- 67% on the average ($n = 1824$; largest percent error at low discharges), and annual total runoff is accurate to +/- 9 %, 2003-2008. Comparison of gauging station versus Water Balance Model (WBM) discharge indicates a small positive model bias; the observed errors of annual runoff values are also positive and are subject to improvement by bias removal. The results indicate that model-based rating curves can provide accurate calibration of remote sensing measurements of discharge. However, an analysis of an exceptional large flood event, along the Indus River in 2010, shows that WBM does not capture flood wave attenuation by overbank flow, and thus predicts faster flood wave celerity and higher peak discharge compared to remote sensing observations. Better modeling incorporating these and other processes will improve conversion of remote sensing measurements of rivers into accurate discharge, including for extreme events.
1. Introduction

Measurements of river discharge and watershed runoff are essential to water resources management, efficient hydropower generation, accurate flood prediction, and improved understanding of the global water cycle. River discharge at-a-site is an integrated signal of water cycle processes over the catchment area upstream, and large amounts of variability over relatively small amounts of time commonly occur. This makes high frequency measurements necessary for many rivers (Fekete et al., 2012). Major efforts have been made to improve the international availability of ground-based discharge data, but many nations do not share hydrological data, and the network of ground stations on a global basis is inadequate. Rivers and tributary streams transgress political borders, causing downstream nations to experience severe constraints in predicting surface water incoming from upstream. Global hydrological modeling can assist in evaluating runoff (Littlewood et al., 2003; Sivapalan et al., 2003), but such modeling is still not sufficiently accurate at high spatial and temporal resolution (e.g. Cohen et al., 2011).

Space-based observational approaches for direct, sustained measurement of river discharge and runoff have so far been little utilized. Yet they are now feasible, using existing and planned sensors. New processing techniques using frequent-revisit microwave-frequency sensing have demonstrated a capability to track discharge changes via sensitive measurement of water surface area changes. Such information can be obtained globally and in "near real time" (within several hours after satellite overpass), but these data require some method of calibration to discharge. Here we employ a global water balance runoff model (WBM) to calibrate
remote sensing to discharge: at satellite river measurement sites within the U.S. that are coincident to comparison ground gaging stations. Error analysis indicates that model-based calibration of the remote sensing signal can substitute for calibration by ground-based discharge data without significant loss of discharge accuracy.

2. Measuring Discharge and Runoff From Space

Previous work demonstrates that orbital remote sensing has the capability to measure river discharge variation in a manner closely analogous to its measurement at ground stations (Brakenridge et al., 2005; Brakenridge et al., 2007; Khan et al., 2011; Smith, 1997; Smith et al., 1996; Temimi, 2011). For ground gauging stations, frequent or continuous river stage height measurements are calibrated to discharge using infrequent, current meter traverses. These intermittent measurements obtained by field surveys sample flow velocities and channel cross sectional areas under varying flow conditions, as stage values are recorded. Empirical, “rating curves” that relate stage to discharge are thereby developed. Such relations allow transformation of continuing, automated stage measurements at each station to the needed discharge values, to an accuracy of 5-10% (Hirsch and Costa, 2004).

National water ministries worldwide use a similar approach (Olson and Norris, 2007; Rantz and others, 1982; Schmidt, 2002).

For measurement via orbital remote sensing method, consider the flow continuity equation:

\[ Q = wdu \]  

(1)
where $Q$ is discharge in m$^3$/sec, $w$ is flow width (m), $d$ is flow depth (m), and $u$ is flow velocity (m/sec). Inherent to flow continuity is that measurements which monitor flow width also provide a proxy indicator of changing discharge (unless the channel banks are vertical). Along most rivers, $w$ is similar to $d$ in its sensitivity to discharge change (Bjerklie et al., 2004); both are more robust predictors of discharge than $u$. Thus, $w$ measurements can be transformed, via a rating curve, to actual discharge, if calibration estimates of actual high, medium, and low discharges can be obtained while sustained width observation is underway (Brakenridge et al., 2007).

As is the case for stage-based gauging stations on the ground, the local river and floodplain channel geometry control the accuracy of rating curve relations in a satellite-based approach. For gauging stations, a desirable site exhibits stable channel geometry with relatively permanent and steep channel banks, where discharge changes are accommodated mainly by changes in flow depth and stage. For observation via satellite, instead, it is width changes that can be most easily observed, and a desirable measurement site is one where mainly width changes occur with variable discharge. Most river systems exhibit reaches of both types. Some rivers are in fact very difficult to monitor by fixed gauging stations: because of variable channel geometry, meandering or braiding channels, and other dynamic processes. Remote sensing offers a complementary approach for these rivers, as a reach area method is less sensitive to such noise.

In this regard, there are actually two alternatives for sensing changes in river “width”: 1) measurement of actual flow width changes, at individual cross sections
(Bjerklie et al., 2003), or 2) remote sensing signal measurements that are sensitive
to flow area change, along a defined measurement reach (Smith, 1997). Monitoring
water surface area is particularly attractive, because the areal averaging of the river
width reduces the uncertainties in the actual river width variations, while taking
advantage of the spatial coverage provided by remote sensing. Reach surface water
area is also less prone to local variation in riverbed geometry. In contrast,
measuring flow width is observationally demanding, because of the dual challenge
of high spatial resolution and frequent sampling in time. Furthermore, high-
resolution characterizations of a river at specific cross sections would require
frequent recalibration due to seasonal, annual, and inter-annual changes in
riverbed, location, and meandering patterns (just as stage rating curves do). This
paper employs the second approach, which is most appropriate for remote sensing
from above: flow area within a defined reach, which allows the use of frequent-
revisit but lower spatial resolution data.

Instead of being observed, river discharge can also be modeled: by
parameterization of catchment areas and measurement of forcing variables,
including precipitation. This offers an opportunity for calibration of remote sensing
signals by using independent model output. Through modeling, if changing
catchment precipitation, soil moisture, evapotranspiration, and other upstream
watershed characteristics can be measured or constrained, reasonably accurate
discharge can be estimated and for potentially unlimited locations along a river. As
daily precipitation and other data fields are ingested, updated model-based
discharge estimates can be calculated at the same time intervals. Contemporary
watershed runoff modeling uses advanced computational capabilities to scale to relatively fine scale watershed characterization (e.g. to a global grid at approximately 10 km). This paper examines the possibility that model-based discharge information can provide the needed calibration of remote sensing observations. Such capability would enable satellite measurements of river discharge via either flow area or stage, and where in situ data are not unavailable.

Here, we analyze a suite of 6 river measurement sites within the U.S. where surface gauging station, remote sensing, and model results are co-located. To begin, we examine the general issue of the temporal sampling needed to adequately characterize river flow variation. Next we describe the passive microwave remote sensing methods that provide the needed measurements. To test the ground-based versus model-based calibration outcomes, we employ a global discharge prediction model (Water Balance Model, WBM) (Vörösmarty et al., 1989) to obtain predicted discharges for the measurement sites. Rating equations for the remote sensing signal are developed and compared via two different methods: 1) using modeled discharge values, and 2) using measured discharge. The co-location with gauging stations also allows constraints to be placed on the accuracy and precision of satellite-based discharge measurements using either approach.

3. Temporal Sampling for Discharge Characterization

For measurement of river discharge (m³/sec), and watershed runoff (mm/t, calculated from discharge, using watershed area), the highly dynamic nature of this phenomenon must be considered. The task is more similar to accurate
measurement of rainfall than to measuring slowly varying terrestrial surface
observables such as vegetation greenness. Thus, highly accurate “spot”
measurements of precipitation rates have relatively little value other than for
calibration: what is needed is relatively continuous surveillance, so that accurate
total amounts can be computed. The same is true for river runoff and discharge.

Presently, earth-observing satellites are being planned to help measure global
river discharge and water storage changes and constrain runoff modeling (Alsdorf
et al., 2003; Alsdorf et al., 2007; Durand et al., 2008; Durand et al., 2010). Potential
remote sensing revisit frequencies for any given river location vary widely: from
hourly, for geostationary satellites, to ~ weekly, for low latitude locations in the
proposed Surface Water and Oceans Topography (SWOT) mission (Biancamaria et
al., 2010). Because of the constellation of sensors currently available, there are clear
opportunities for complementary measurements, in which more-precise but
relatively infrequent observational data from specific missions such as SWOT can be
combined, when available, with less precise but ongoing and frequent surveillance
of rivers by operational systems.

The minimum temporal sampling needed to adequately characterize river flow
varies with river flow regime. Along some very large rivers, where the daily
discharge is strongly auto-correlated and the rate of change is not fast, sampling
frequency requirements may not be high. As a result, except during major flooding,
surface stations that provide a daily record may actually oversample along large
rivers. However, water discharge for most rivers is a rapidly varying flux, at least
during part of a season (Shiklomanov et al., 2006). Thus: 1) a 10-fold discharge
change may occur along many rivers over a period of only several days, or less, and
2) a large proportion of total annual river runoff may be concentrated in flood
seasons lasting only several weeks to several months. Also, measuring low flow
during a sustained drought, or high flow during a flood, requires sustained high
frequency observation: the duration of extreme flow in days is as important as high
precision individual measurements in obtaining total monthly runoff. Shiklomanov
et al (2006), analyzing Arctic rivers, describe in detail this strong dependence on
sampling frequency in measuring accurate values for even total annual runoff.

Although stage-discharge rating curves exhibit various errors, including
hysteresis (Dottori et al., 2009), transformation of frequently or continuously
measured stage to estimate discharge has long been accomplished within acceptable
and well-constrained accuracy and precision. An inherent motivation of this overall
approach is to provide close-interval sampling in time. In some cases (e.g. flood
hydrographs along smaller rivers), the time scale may be hours, but the large
proportion of ground station-based river discharge data is reported using daily time
intervals. An important challenge for remote sensing of river discharge is, therefore,
to achieve at least this same frequent sampling in time while progressively
improving, with better sensors and processing techniques, the accuracy of
individual (daily) measurements.

4. Passive Microwave Radiometry for River Discharge Measurement

One reason for utilizing microwave information is that, at selected
frequencies, microwave radiation suffers relatively little interference from cloud
cover. Also, night overpasses can be utilized, and the signal is independent of solar illumination. These attributes allow for frequent and repeatable data retrievals.

Factors that affect total microwave brightness temperature from a mixed water and land surface measured by an image pixel include: a) sensor calibration characteristics (stability of its signal through time), b) perturbation of the signal by land surface changes (e.g., physical temperature, soil moisture, crop changes, snowfall, and rainfall), and c) contrast between land and water (very different values of effective emissivity for water and land favor the most sensitive monitoring of water area change). Also, microwave frequencies have more commonly been used to observe soil moisture changes (Schmugge, 1980; Theis et al., 1982; Ulaby et al., 1978; Wang et al., 1982; Wang et al., 1980). Because of the sensitivity of microwave emission to soil moisture, as well as to surface water, measurements of surface water change must incorporate some method to account for variations caused by temporal changes in soil moisture.

The fundamental basis of passive microwave sensitivity to river discharge was analyzed with a microwave emission model derived from first principles (Brakenridge et al., 2007). The emission model is developed from fluctuation-dissipation theory, incorporating non-isothermal conditions of riverine environments. Correlations of electromagnetic fields derived from Maxwell's equations with different polarizations can be cast in form of a hyperbolic cotangent factor of the quantum energy (ħω) over the absolute physical temperature (Tsang et al., 1985), operated on a tensor product involving the polarization vector, complex effective permittivity, and dyadic Green’s function (Nghiem et al., 1990).
A difficulty in interpreting the brightness temperature measured by a satellite radiometer is that it is a product of both physical temperature and emissivity. Whereas the emissivity contains water information, the physical temperature can change quickly, depending on time of the day, solar shading (e.g., topographic shadowing), and weather conditions. Whereas many passive microwave methods use the polarization ratio (PR) and the frequency gradient ratio (GR) to cancel physical temperature within a pixel, PR and GR also reduce the sensitivity to water change (Brakenridge et al., 2007). The key for river discharge measurement is to cancel the physical temperature, also using a ratio approach, but with the river measurement pixel amplitude value compared to nearby but separate calibration pixel values. This approach retains a high sensitivity to river discharge variability expressed as water surface area changes (Brakenridge et al., 2007).

Finally, the reach water surface area approach also greatly relaxes the spatial resolution requirements for sensing flow width variation. The microwave signal from a defined river reach, and geographically including both: a) lower channel water area, and b) upper channel bar surfaces and floodplain dry land, will track discharge: as the river rises and falls, the water and land proportion within the reach changes, and only a sensitive numeric indicator of such is needed. An actual map of water versus land is not required. The microwave signal variation from individual, relatively large (~ 10 km) pixels centered over rivers can thus be used directly (Brakenridge et al., 2007). This approach in fact requires relatively large image pixels, because it is important that the largest floods not completely fill or saturate a pixel. The sensitivity, noise characteristics, and stability of the remote
sensing signal are, however, critical, and the remote sensing data must also be accompanied by high quality geocoding: any variation in the actual ground surface being sampled by repeat measurements introduces noise.

5. Geographic Sampling Considerations for Global Measurements

For global characterization of freshwater runoff through rivers, a large array of sites, at least several thousand, is needed: this still provides only several hundred per continent and leaves many major streams and rivers un-monitored. There are many potential issues involved with efficient design of stream-flow gaging station networks sampling global scale land areas. For example, although relatively few gauges located near the mouths of large rivers can capture a considerable portion of the total discharge to oceans (Fekete et al., 2002), the remaining contributing landmasses are increasingly fragmented into hundreds of small watersheds. Also, discharge should best measured just downstream of the confluences of tributaries, because discharge changes only gradually along trunk streams, whereas tributaries typically add a large sudden increment that is important to capture.

Design criteria for global sampling schemes are beyond the scope of this paper. However, previous MODIS imaging of global surface water variability (Brakenridge et al., 2005; Brakenridge and Kettner, 2012) provides abundant (n=2583) suitable locations where flow area variation has already been measured optically on an intermittent basis (Figure 1). At these locations, it has been demonstrated that a water area-sensitive remote sensing signal will monitor flow variability. They are thus a useful stating point in designing a global array.
Microwave signal data for these and approximately 4000 additional sites (De Groeve, 2010; De Groeve et al., 2006; De Groeve and Riva, 2009; Kugler and De Groeve, 2007) added more recently are available at:

http://www.gdacs.org/flooddetection/. We emphasize that: a) the sensitivity of each measurement site to discharge variation, and b) the shape and position of each site’s signal/discharge rating curve, are both a function of individual site characteristics, and especially channel and floodplain morphology. Thus is posed the challenge to develop an efficient signal-to-discharge calibration approach.

6. Choice of Data and Processing Strategies

The remote sensing data available to monitor rivers in the microwave domain includes the 37 GHz channel provided by the SMMR (Scanning Multichannel Microwave Radiometer) in 1978-1987, the SSM/I (Special Sensor Microwave Imager) aboard the Defense Meteorological Satellite Program satellite series (1987 to present), the 37 GHz channel aboard TRMM (Tropical Rainfall Measurement Mission, 1998 to present), and similar frequency but including V/H polarimetric data provided by AMSR-E, (Advanced Microwave Scanning Radiometer for Earth Observation System) July, 1, 2002-October 4, 2011. The data from these sensors are freely available to the public in swath image formats (not geolocated into map projections, but with accompanying latitude and longitude coordinate information for each pixel) and also as geocorrected raster images (pixels of fixed dimensions and geographic location within global or large-region raster files).
In this study, we describe two passive microwave data sources and also two
signal processing methods. However, our model/gauging station/remote sensing
comparisons use mainly one approach: AMSR-E data processed according to the
first method, below, which was used prior to transition to the second method in the
current processing scheme.

Method 1 uses AMSR-E 36.5 GHz, horizontal H polarization, descending orbit
(night) data, as obtained by a swath image pixel value retrieval algorithm (De
Groeve et al., 2006). Data from within a 5 km radius of a geographic point target are
retrieved, and as determined by the geolocation information for each pixel (values
obtained are from pixels whose centroids are within that radius). The river
measurement reaches (the “M” data) are, therefore, circular in shape. Also,
information from a fixed and nearby (dry land) comparison site (the “C” data) is
retrieved from the same swath image and includes an area of identical size,
manually selected to be free from mapped streams and rivers. M/C, a dimensionless
ratio value, is the discharge estimator; as noted, use of the ratio isolates any change
that affects only one of the pixels and, in particular, river flow area variation. These
data obtained in this way commonly show a strong correlation to measured
discharge at many sites in the U.S. (Figure 2A, Figure 3).

Method 2 uses AMSR-E 36.5 GHz, total amplitude (V and H polarizations
combined), and including data from both ascending and descending orbits, as
mosaicked within georeferenced, global-coverage, near real time raster images.
These image data are in latitude and longitude (Plate Carree) projection, with pixel
dimensions of .0833 degrees (approximately 9.27 km square at the equator but
with decreasing east-west km dimensions at increasing distances from the equator).

The processing, as automatically performed by the Global Flood Detection System in Ispra, Italy (De Groeve, 2010; De Groeve and Riva, 2009), also calculates a dimensionless ratio value from these rasters, but the comparison value is based on the brightest (driest) values from a 7 x 7 pixel array in the raster and centered on the measurement pixel. The measurement pixels each contain the same latitude and longitude point targets as for the first method, but the fixed pixel ground footprint means that the river reach being sampled differs significantly (with a maximum shift of a half pixel size, or about 5 km). This approach does not require the manual selection of the calibration pixel, making it computable anywhere in the world. Its other advantage is that single-pixel variation in the calibration information cannot so strongly affect the discharge-estimator signal. In detail, the algorithm calculates the (95th percentile) brightest value of the calibration pixels and the ratio of that value to the measurement pixel value (Figure 2B, Figure 3). Previous comparisons of the two methods for other sites indicate the results to be strongly correlated (Figure 2) and to exhibit comparable amounts of scatter and error (De Groeve and Riva, 2009).

In both processing methods, a 4-day forward running mean is applied, because AMSR-E does not provide daily revisits at lower latitudes. Instead, some locations commonly are revisited every two days, or, rarely, only every three days, as the AMSR-E orbit precesses. The 4-day running mean facilitates a most-current update, daily, with values for every location globally. In any comparisons to ground station data or model output, therefore, we also use 4 day running mean data.
Future microwave sensors such as NASA’s planned GPM mission will provide more-than-daily revisits and thus a daily update without multi-day averaging will be possible.

The AMSR-E data offer the capability to consistently monitor river measurement sites for nearly a decade (data begin in July, 2002) and for ground footprints of approximately 10 km; however, the sensor ceased operation on October 4, 2011. The 37 GHz frequency and H polarization were selected in method because H polarization data exhibits the strongest differential response to water and land (Brakenridge et al., 2007) at this frequency and with lesser sensitivity to soil moisture. The ongoing TRMM satellite output provides similar microwave data (but from a non-polar orbit, and without high latitude coverage). The signal processing at GDACS/GFDS is presently using these TRMM data; the methods described may also be applicable to an array of similar frequency remote sensing from other sensors.

7. The WBM global hydrology model

The WBM model includes the water balance/transport model first introduced by (Vörösmarty et al., 1998; Vörösmarty et al., 1989) and subsequently modified (Wisser et al., 2010; Wisser et al., 2008). WBM is a relatively simple but robust water budgeting scheme that takes into account climate forcings (air temperature and precipitation in its simplest form) and estimates various water stocks (soil moisture and groundwater) and fluxes (evapotranspiration, surface runoff, groundwater recharge and baseflow). WBM has been applied successfully in
small watersheds at 200m spatial resolution, up to a global scale at 6 minute grid cell sizes. WBM was probably the first hydrological model applied to a global domain. Perhaps the main difference between WBM and comparable large-scale hydrological models is the high degree of flexibility in specifying computation domains and input data and configuration. WBM has demonstrated a bias of 5-8mm/yr (Fekete et al., 2002; Vörösmarty et al., 1998) with respect to annual runoff (297mm/yr). Numerous studies have shown that the most critical input variable is precipitation (Fekete et al., 2004; Biemans et al. 2009).

At its core, the surface water balance of non-irrigated areas is a simple soil moisture budget expressed as:

\[
\frac{dW_s}{dt} = \begin{cases} 
-g(W_s)(E_p - P_a) & P_a \leq E_p \\
P_a - E_p & E_p < P_a \leq D_{WS} \\
D_{WS} - E_p & D_{WS} < P_a
\end{cases}
\]

(2)

driven by \(g(W_s)\), a unitless soil function:

\[
g(W_s) = \frac{1-e^{-\frac{W_s}{W_c}}}{1-e^{-\alpha}}
\]

(3)

\(W_s\) is the soil moisture, \(E_p\) is the potential evapotranspiration, \(P_a\) is the precipitation (rainfall \(P_r\) combined with snowmelt \(M_s\)), and \(D_{WS}\) is the soil moisture deficit: the difference between available water capacity \(W_c\), which is a soil and vegetation dependent variable (specified externally) and the soil moisture. The unit-less empirical constant \(\alpha\) is set to 5.0 following Vörösmarty et al. (1989).

Flow routing from grid to grid cell follows the downstream grid cell tree
topology (which only allows conjunctions of grid cells upstream, without splitting to form islands or river deltas) and is implemented using the Muskingum-Cunge equation, which is a semi implicit finite difference scheme to the diffusive wave solution to the St. Venant equations (ignoring the two acceleration terms in the momentum equation). The equation is expressed as a linear combination of the input flow from current and previous time step \((Q_{in \cdot t}, Q_{in \cdot t-1})\) and the released water from the river segment in the previous time step \((Q_{out \cdot t-1})\) to calculate new grid-cell outflow:

\[
Q_{out \cdot t} = c_1 Q_{in \cdot t} + c_2 Q_{in \cdot t-1} + c_3 Q_{out \cdot t-1}
\] (4)

The Muskingum coefficients \((c_1, c_2, c_3)\) are traditionally estimated experimentally from discharge records, but their relationships to channel properties are well established. We use a power function approximation of channel geometry \(w = ay^b\), expressing the relationship between the river width \((w)\) as a function of flow height \((y)\) from the river bottom. Exponent \(b\) dictates the ratio of flow velocity and flood wave celerity. Detailed descriptions are available (Wisser et al., 2010).

In this paper, the WBM water discharge predictions are from a daily, global scale simulation at 6 arc-minute spatial resolution (approximately 11 km at the equator). Daily predictions are averaged by a 4 day running mean window to align with the satellite microwave 4 day averaging process. The precipitation dataset is from the Global Precipitation Climate Center GPCC, Offenbach, Germany (gpcc.dwd.de) using their “Full” product, which combines long-term precipitation climatology, derived from the entire data archive, with anomalies estimated from
the operating meteorological stations at any given time. The GPCC “Full” product is available at monthly time steps at 30 arc-minute spatial resolution. Daily partitioning of the monthly precipitation totals was established by computing the daily fraction of the monthly precipitation from the NCEP reanalysis product (Kalnay et al., 1996; Kistler et al., 2001). A six minute topological network (Vörösmarty, Fekete, Meybeck, & Lammers, 2000) was derived from the high resolution gridded network HydroSHEDS using SRTM elevation data set (Lehner, Verdin, & Jarvis, 2008). A comprehensive list of the model input datasets is provided (Cohen et al., 2011).

8. Testing WBM Model Output For Rating Curve Generation

The United States is monitored by a relatively dense array of operational hydrological gaging stations. Data from these allow us to evaluate the effectiveness of a model- instead of gauging station- based approach to calibrate remote sensing measurements to discharge values.

We chose 6 sites for satellite-based measurement in the continental U.S. (Figure 4) that are coincident to or in very close proximity with in situ stations providing daily measurements between 2002-2010. The site locations and attributes represent diverse geomorphological, land-use and climate settings (Table 1). Although this is a relatively small number of sites, their analysis provides the opportunity to consider in detail the relationship of the remote sensing to actual discharge variation and that provided by the model.
For each site, the empirical relation (the rating curve) between the remote sensing signal and ground station-measured water discharge is constructed. As well, the rating curve resulting from comparing only modeled discharge values to the remote sensing data is produced: this would be the only possible method for calibrating thousands of river measurement sites distributed globally (Figure 1), and given the inability to retrieve, for most nations, daily discharge information. We investigate how accurately satellite sensors can measure discharge, if the signal is calibrated only from global modeling results: without any ground-based information.

Three temporally coincident datasets are used in each case (Figure 5):

1. Daily, including the complete (9 year) daily values (n = 3285);
2. Monthly, including the monthly mean, maximum and minimum values (n = 36);
3. Yearly, including the annual mean, maximum and minimum values (n = 27).

For consistency, second-order polynomial rating curves are used to evaluate the scatter plots created in all cases (Table 2). We compared our results using other regression equations without substantial change in the results. Because of relatively large scatter at the lower end of some river discharge regimes (the flow area method becomes less sensitive once flow is fully confined within the lower channel), there is an additional requirement that all portions of the polynomial curve remain monotonic or flat.

We seek to also determine the optimal calibration strategy (daily, monthly or yearly values) that could be applied to a large number of sites. Figure 6 shows daily
water discharge time-series (2002-2010) for the six sites together with model-based and station-measured calibrations. The plots also include the measured discharge at the nearby gaging station (Figure 4 and Table 1) for comparison. The top plot for each site is for the daily calibrations; the middle for calibration with monthly statistics; and the bottom with yearly statistics (e.g., figures 5a, 5b and 5c respectively).

Overall, comparison of the remote sensing signal data to station-measured discharge (blue lines in all figures) yields, visually, a generally strong time series correlation to gauged discharge (black lines). Also, discharge estimation based on daily data calibration (rating curves) is quite similar to that obtained when the rating curve uses monthly and yearly statistics: if station data are used for the rating curve; Figure 6).

Discharge prediction derived from model-based calibration (dashed orange lines in Figure 6) varies depending on whether daily versus yearly or monthly data are used for the rating curves. Daily data-based rating equations in this case predict lower than observed discharge (most clearly in site #530), whereas monthly and yearly statistic-based calibrations and rating curves provide more accurate results. Comparison of WBM model results to measured discharge further indicates that the model itself generally under-predicts mean discharge (Table 1). In sites #997 and #2483, the daily data-based rating curve produces more accurate results than monthly and yearly calibrations. In these two cases, WBM considerably over-predicted high discharge events (Figure 6). The results overall demonstrate the sensitivity of any model-based calibration approach to the accuracy of the model.
predictions. They also clearly indicate that using yearly and monthly statistics to calibrate the AMSR-E signal data to discharge better characterizes extreme discharge events: even though, for some events, there is over-estimation of the flood magnitude (i.e. sites 997 and 2483; Figure 6). Finally, they indicate that model-based calibration, in general, is a viable approach for translating the flow-area signal to discharge.

To also evaluate the current data and processing method (method 2) for one example, daily station-measured and remote sensing-measured values (n = 1824) were obtained for site #524, 2003-2006 and using the model-based rating curve. Assuming the gauging station data as representing true discharge, the average error (departure) of the remote sensing discharge values is 67%, with percentage errors being largest at times of low flow. The relatively large daily value errors are reduced in the calculation of runoff totals from these data. For annual values 2003-2008, the average error is 9%. Previous work (Brakenridge et al., 2007) indicates one source of error in the daily values is the lack of exact temporal match between the station and remote sensing discharge series. For example, major flood peak discharge as measured by surface gauging stations may precede by several days the peak recorded by remote sensing (which is measuring reach flow area, over a relatively large area). Such lags produce a negative departure (remote sensing value – station value) as the peak flow passes the station and while the reach area is progressively flooding. Then, several days later, a positive error occurs as stage is already declining at the station (in part due to the overbank flow). Thus, the peak value may be recorded fairly accurately by both ground-based stage and satellite-based flow.
area techniques, but the timing may differ and lead to increases in the average daily measurement error.

**9. Remote Measurements of the 2010 Indus River flood, Pakistan**

As noted, for many locations globally, daily discharge information from surface gauging stations is difficult or impossible to obtain. Even where gauging station data are available and are public, large floods can temporarily damage or entirely disable surface stations. We have demonstrated that orbital remote sensing can, presently, provide valuable river discharge information and monthly and annual runoff volumes. However, there are, clearly, significant errors still to be addressed (examine the time series shown in figures 3 and 6). Perhaps the greatest asset of the remote sensing capability here detailed is its ability to be quickly and easily applied to new measurement sites of interest, without field access. An example allows further examination of the utility of satellite microwave river discharge measurements in general, and those based on WBM model calibration in particular.

During the summer monsoon of 2010, the upstream Khyber-Pakhtunkhwa region of Pakistan experienced rainfall totals >300 mm July 27-30, and the Punjab, Gilgit Baltistan and Azad Kashmir provinces received July rainfall totals of >500 mm. The trunk stream (Indus) flood hydrograph then traversed 500 km of river reach to the sea, mainly along a meandering channel that is constrained within a 15 to 20 km wide floodplain by engineered artificial levees (Syvitski and Brakenridge, submitted). All of this floodplain, and more, was inundated. Analysis of optical
remote sensing data indicates that most damage was caused by multiple failures of irrigation system levees, and by barrage-related backwater effects that initiated failures and led to avulsions (sudden changes in flow location). A detailed analysis is provided elsewhere (Syvitski and Brakenridge, submitted). Attention is directed here to the difference between the modeled and the remotely-observed flood hydrograph at an illustrative remote sensing measurement site (site #2010; Figure 7).

The WBM-modeled peak discharge for this event at site #2010, south of the major levee failure and avulsion at the Tori Bund, is ~26,000 m³/sec, with flow being elevated above 15,000 m³/sec for only several days (Figure 7). However, the model includes no limitations on the volume of water transported in a river at a point in time (no change to overbank flow conditions is incorporated). This can cause over-prediction of the magnitude of high flow events (as shown in the U.S. sites #997 and #2483; see also Cohen et al., 2011). Also, the modeled water is transported much too rapidly downstream. A new version of WBM (currently in testing) will address these limitations by incorporating an over-bank flow component that acknowledges the reality of channel overtopping during large discharges. Also, the present model does not include the possibility of avulsion.

Comparison of the remotely sensed discharge at station #2009, upstream of the avulsion at Tori, and at #2010 indicate a reduction of measured peak flow downstream of the breach by ~10,000 m³/sec (Syvitski and Brakenridge, submitted). Figure 7 shows as well the very different shape of the observed hydrograph at this site compared to that modeled for it. Thus, avulsion reduced the
peak flow, and, also, the flood was experienced for much longer (22 days of > 15,000 m³/sec) than the model predicted. During large floods, and even along heavily engineered rivers, major attenuation of the flood wave typically occurs, and this is illustrated in the Indus example. This attenuation can, clearly, be measured in detail by this form of remote sensing. Its adequate characterization by modeling at this spatial scale remains an important task for future work.

10. Conclusion

The results indicate that microwave satellite measurements at carefully selected river reaches can approach in-situ ground station information in their utility for several applications of river runoff and discharge information, including the analysis of daily flood dynamics and the quantification of longer term watershed runoff volumes. However, remote sensing of rivers through these methods does require some form of calibration to discharge values via rating equations. The examples we analyzed indicate that the needed transformation of water-area sensitive remote sensing to river discharge can be accomplished by incorporation of global runoff model results. Using the described or similar microwave data and processing approaches, and for river measurement sites whose channel and floodplain morphologies favor flow area variability, 4-day running mean daily discharges as measured via satellite compare favorably with information obtained by gauging stations. The timing and duration of periods of high and low flow are accurately constrained, and the relative magnitude in m³/sec of flood peaks can be determined. However, daily value accuracies exhibit significant errors, in part due to a lack of exact temporal match in the timing of some major flood peaks. For
annual runoff expressed in mm/yr, observed errors at the suite of sites examined
and using a global model-based calibration approach was relatively small. This
suggests that the measurement technology is already able to deliver significant new
information for water balance studies at many international locations, and without
support by ground-based information.

We stress the synergy between remote sensing altimetry approaches and
flow area approaches for discharge measurement. One upcoming space agency
mission (the U.S./France SWOT satellite) is being designed to provide global data
sets of accurate swath radar altimetry-based river stage and slope, but without a
long-term record and with a short (3-year) nominal mission life. Flow area
measurements through existing and planned microwave sensors can, meanwhile, be
made frequently (~ daily); they can be extended back about three decades in time,
and they can be continued while SWOT is collecting data and afterwards. Several
satellites are currently providing appropriate, stable, well-calibrated, water area-
sensitive data; these can now be being used to measure river discharge changes. For
many research efforts and well as practical applications, both long-term data and
current near-real-time observations are necessary. The challenge is to develop
processing methodologies that can ingest, process, and disseminate the results, and
provide reliable error estimates, and then to allow synergistic incorporation of
altimetry data when such become available.

In regard to the best calibration/rating curve approaches, our analysis
indicates significant variation in the rating curve equations, depending on whether
daily datasets or monthly or yearly statistics are used. In general, daily data-based
rating curves do not always accurately estimate the highest flow events: polynomial
or other regression techniques applied to the comparisons of modeled and observed
daily data may not accurately capture the relation between the largest discharge
and the remote sensing signal, and especially as long as the modeled routing of flood
waves inadequately captures overbank and other flow attenuation processes.
Rating curves based instead on monthly or yearly maximum and minimum statistics
better characterize the signal/discharge relation at the extremes. Preliminary work
using the method 2 data and processing indicates that incorporating a 5 year period
of record for both modeled and observed values, and using monthly daily maxima,
minima, and mean values (n =180) commonly produces rating curves with second
order polynomial least square regression r^2 values >.6 at favorable sites, and also
provides more accurate prediction of peak flow values.

11. References

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Table 1. Characteristics of 6 remote-sensing sites and corresponding USGS gaging stations (Figure 1) and the Indus site and gaging station (Figure 5). Site mean discharge is as predicted by WBM.

<table>
<thead>
<tr>
<th>Site ID</th>
<th>Site River Name</th>
<th>Site Coordinates Lat/Long (dd)</th>
<th>Site Drainage Area (km²)</th>
<th>Site Mean Discharge (m³/s)</th>
<th>Station ID</th>
<th>Station Coordinates Lat/Long (dd)</th>
<th>Station Drainage Area (km²)</th>
<th>Station Mean Discharge (m³/s)</th>
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<tr>
<td>507</td>
<td>Missouri, Brunswick</td>
<td>39.34/-93.02</td>
<td>1,264,731</td>
<td>1206</td>
<td>06906500</td>
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<td>1709</td>
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<td>524</td>
<td>White, Newberry</td>
<td>38.91/-87.07</td>
<td>12,802</td>
<td>161</td>
<td>03360500</td>
<td>38.92/-87.011</td>
<td>12,137</td>
<td>182</td>
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<tr>
<td>530</td>
<td>Red, Halstad</td>
<td>47.26/-96.84</td>
<td>65,000</td>
<td>39</td>
<td>05082500</td>
<td>47.92/-97.029</td>
<td>77,929</td>
<td>170</td>
</tr>
<tr>
<td>925</td>
<td>Willamette</td>
<td>45.18/-123.01</td>
<td>19,710</td>
<td>504</td>
<td>14191000</td>
<td>44.94/-123.042</td>
<td>18,928</td>
<td>591</td>
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<tr>
<td>997</td>
<td>Connecticut</td>
<td>41.84/-72.632</td>
<td>26,240</td>
<td>500</td>
<td>01184000</td>
<td>41.98/-72.606</td>
<td>25,116</td>
<td>567</td>
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<td>2483</td>
<td>Pee Dee</td>
<td>33.82/-79.32</td>
<td>28,706</td>
<td>336</td>
<td>02135200</td>
<td>33.66/-79.155</td>
<td>36,660</td>
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<td>2010</td>
<td>Indus, Hala</td>
<td>25.9/68.26</td>
<td>1,070,050</td>
<td>2730</td>
<td>Mandi Plain</td>
<td>31.75/74.75</td>
<td>20,886</td>
<td>497</td>
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Table 2. Rating curves equations of AMSR-E C/M radiance ratios versus WBM-predicted and gaging station-measured discharge with daily, monthly and yearly statistics (Figure 2). Site ID corresponds to Table 1 and Figures 1 and 5.

<table>
<thead>
<tr>
<th>ID</th>
<th>USGS daily</th>
<th>WBM daily</th>
<th>USGS monthly</th>
<th>WBM monthly</th>
<th>USGS yearly</th>
<th>WBM yearly</th>
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</thead>
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<tr>
<td>507</td>
<td>530.71x² + 9092.7x</td>
<td>-4740.5x²</td>
<td>1377.1x² + 9526.3x</td>
<td>25418x² - 42215x</td>
<td>7548.9x² - 8277.2x</td>
<td>18291x² - 26997x</td>
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<td></td>
<td>- 9356.7</td>
<td>+ 20231x-15676</td>
<td>- 10485</td>
<td>+ 16604</td>
<td>+ 1349.9</td>
<td>+ 8637.6</td>
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<td>524</td>
<td>1895.9x² - 3321.3x</td>
<td>-253.99x² +</td>
<td>-559.11x² +</td>
<td>935.9x² - 344.86x</td>
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<td>-22.769x² +</td>
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<td>+ 1503.2</td>
<td>1280.3x - 951.57</td>
<td>3004.7x - 2320.3</td>
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<td>248.38x² - 210.5x</td>
<td>3413.6x² -</td>
<td>1514.8x² - 1969x -</td>
<td>3044.7x² - 4616.2x</td>
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<td></td>
<td>+ 4062.1</td>
<td>- 11.181</td>
<td>5463.7x + 2180.9</td>
<td>+ 555.27</td>
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<td>12268x² - 26478x</td>
<td>5719.4x² - 10142x</td>
<td>6893.6x² - 12527x</td>
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<td></td>
<td>+ 14607</td>
<td>+ 4382.4</td>
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<td>+ 12111</td>
<td>7989.8x - 7354.3</td>
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<tr>
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<td>17051x² - 34488x</td>
<td>10897x² - 21890x</td>
<td>22195x² - 42451x</td>
<td>40085x² - 78585x</td>
<td>29201x² - 57348x</td>
<td>57460x² -</td>
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<tr>
<td></td>
<td>+ 17789</td>
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<td>+ 20421</td>
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<tr>
<td>2483</td>
<td>21959x² - 41141x</td>
<td>17858x² - 33431x</td>
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<td>+ 12726</td>
<td>+ 28870</td>
<td>+ 14093</td>
<td>+ 34948</td>
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Figure 1. Satellite river measurement sites (n = 2583) where optical remote sensing (2001-2010) detects significant surface water area variation within the site reaches (10 km in length). Near-daily time series of passive microwave signal have been obtained and archived for each site since July 1, 2002. Evaluation of the 10 yr+ time series allows the daily signal data to be binned into low flow (yellow dots), normal flow (blue dots), moderate flood (purple dots, recurrence interval > 1.33 yr via Log Pearson III) and large flood (red dots, > 5 yr recurrence). Red dots at high latitudes are processing errors due to ice-covered conditions.
Figure 2. A (top), Plot of the microwave discharge estimator ratio, 4-day running means, calculated according to method 1, for each day, January 1, 2009 - December 31, 2010, versus 4-day forward running mean gauging station discharge, White River, southern Indiana (remote sensing site 524; gauging station USGS 03360500 White River at Newberry, Indiana). B (bottom), Plot of the estimator ratio, calculated according to method 2, versus the gauging station information, same time period.
Figure 3. A, top: satellite-estimated daily 4-day running mean river discharge, site 524, in red, compared to 4-day running mean discharge measured at the co-located gauging station (blue). Rating curve was based on comparison of daily station and (method 2) satellite data. B, bottom: satellite-estimated discharge, red, using a rating based on the WBM model-produced discharge information (same remote sensing data). The model-based rating curve underestimates peak discharge but characterizes average flow conditions quite accurately. Vertical scales are in ft$^3$/sec.
Figure 4. Location map for this paper’s sample of remote sensing river measurement sites and co-located USGS gaging stations.
Figure 5. Example plots (site #925) of method 1 microwave discharge estimator values versus WBM-simulated discharge. A, top: Daily values using the entire dataset. B, middle: Monthly values (monthly mean, minima and maxima). C, bottom: Yearly values, using only yearly mean, minimum and maximum. The daily value-based rating equation underestimates flood flows.
Figure 6. Nine year (2002-2010) daily time series of water discharge for the 6 remote-sensing sites (numbering corresponds to Figure 4 and Table 1). Gauging station-measured discharge is plotted with a thick black line, microwave signal-estimated discharge based on the gauging station data is plotted with a blue line, and microwave signal-estimated discharge based on WBM model-predicted discharge is plotted with a dashed orange line. The top plot for each site is for calibration using the entire daily dataset, the middle plot is for calibration using only the monthly statistics and the bottom plot for calibration using only yearly statistics.
Figure 6, continued.
Figure 6, continued.
Figure 7. Time series for the year 2010 showing the time lag between WBM-simulated and microwave-observed discharge (dashed black and solid blue lines respectively) at site #2010 on the Indus River, Hala, Pakistan. Modeling predicts an earlier and higher flood crest, and more rapid dissipation than was observed via remote sensing.